

# Joint Asymmetric Loss for Learning with Noisy Labels

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# Motivation

- Learning with noisy labels is a crucial task for training accurate deep neural networks. Robust loss function is a popular approach to solve this problem.
- Active Passive Loss (APL) jointly optimizes an active and a passive symmetric loss to mutually enhance the overall fitting ability.
- Asymmetric losses, a new class of robust loss functions, possess superior properties compared to symmetric losses.
- However, existing asymmetric losses are not compatible with advanced optimization frameworks such as APL.

# Contributions

- We propose a novel asymmetric loss function, ***Asymmetric Mean Square Error (AMSE)***. We rigorously establish the condition for AMSE to satisfy noise-tolerance.
- By incorporating the proposed AMSE into the APL framework, we introduce a novel approach called ***Joint Asymmetric Loss (JAL)***, which ensures robustness and enhances sufficient learning.
- The extensive results highlight the superiority of our method.

# Preliminary

For a loss  $L(f(\mathbf{x}), y) = \sum_{k=1}^K \ell(f(\mathbf{x})_k, e_k)$ :

- **(Active Loss Function)**  $L_{active}$  is an active loss function if  $\forall(\mathbf{x}, y) \in D, \forall k \neq y, \ell(f(\mathbf{x})_k, e_k) = 0$
- **(Passive Loss Function)**  $L_{passive}$  is a passive loss function if  $\forall(\mathbf{x}, y) \in D, \exists k \neq y, \ell(f(\mathbf{x})_k, e_k) \neq 0$

By combining the two different symmetric loss functions, APL can improve the fitting ability under the premise of ensuring robustness.

- Recently, asymmetric loss functions have been proposed, which are noise-tolerant.
- **(Asymmetric Condition).** On the given weights  $w_1, \dots, w_K \geq 0$ , where  $\exists t \in [K], s.t., w_t > \max_{i \neq t} w_i$ , a loss function  $L$  is called asymmetric if  $L$  satisfies

$$\arg \min_{f(\mathbf{x})} \sum_{k=1}^K w_k L(f(\mathbf{x}), k) = \arg \min_{f(\mathbf{x})} L(f(\mathbf{x}), t),$$

where we always have  $\arg \min_{f(\mathbf{x})} L(f(\mathbf{x}), t) = \mathbf{e}_t$ .

- In this paper, we extend the asymmetric loss function to a more complex passive loss scenario and propose the Asymmetric Mean Square Error (AMSE).
- **Asymmetric Mean Square Error (AMSE)**

$$L_{\text{AMSE}} = \frac{1}{K} \| a \cdot \mathbf{e}_y - f(\mathbf{x}) \|_2^2$$

- **Theorem (Noise-tolerant for AMSE).** On the given weights  $w_1, \dots, w_K$ , where  $w_m > w_n$ , and  $w_n = \max_{i \neq m} w_i$ . The loss function  $L(f(\mathbf{x}), y) = \frac{1}{K} \| a \cdot \mathbf{e}_y - f(\mathbf{x}) \|_q^q = \sum_{k=1}^K \frac{1}{K} |a \cdot e_k - f(\mathbf{x})_k|^q$ , where  $q > 0$  and  $a \geq 1$  are parameters, is asymmetric if and only if  $\frac{w_m}{w_n} \geq \frac{a^{q-1} + \sum_{i \neq m} \frac{w_i}{w_n}}{(a-1)^{q-1}} \cdot \mathbb{I}(q > 1) + \mathbb{I}(q \leq 1)$ .

# Methodology

We integrate the proposed AMSE into the APL framework to enhance its performance, resulting in a novel approach called **Joint Asymmetric Loss (JAL)**.

- By combining Normalized Cross Entropy (NCE), we have JAL-CE:

$$L_{\text{JAL-CE}} = \alpha \cdot L_{\text{NCE}} + \beta \cdot L_{\text{AMSE}}$$

- By combining Normalized Focal Loss (NFL), we have JAL-FL:

$$L_{\text{JAL-FL}} = \alpha \cdot L_{\text{NFL}} + \beta \cdot L_{\text{AMSE}}$$



# Experiments

Table 3. Last epoch test accuracies (%) of different methods on CIFAR-10 and CIFAR-100 with clean, symmetric ( $\eta \in [0.2, 0.4, 0.6, 0.8]$ ), and asymmetric ( $\eta \in [0.1, 0.2, 0.3, 0.4]$ ) label noise. The results (mean $\pm$ std) are reported over 3 random trials and the top-2 best results are in **bold**.

CIFAR-10	Clean	Symmetric				Asymmetric			
		0.2	0.4	0.6	0.8	0.1	0.2	0.3	0.4
CE	90.50 $\pm$ 0.22	75.21 $\pm$ 0.39	58.05 $\pm$ 0.53	38.80 $\pm$ 0.45	19.74 $\pm$ 0.40	86.85 $\pm$ 0.15	83.05 $\pm$ 0.35	78.37 $\pm$ 0.61	73.85 $\pm$ 0.07
FL	89.70 $\pm$ 0.24	74.50 $\pm$ 0.18	58.23 $\pm$ 0.40	38.69 $\pm$ 0.06	19.47 $\pm$ 0.74	86.64 $\pm$ 0.12	83.08 $\pm$ 0.07	79.34 $\pm$ 0.30	74.68 $\pm$ 0.31
GCE	89.36 $\pm$ 0.19	89.36 $\pm$ 0.19	82.19 $\pm$ 0.84	68.01 $\pm$ 0.40	46.61 $\pm$ 0.39	88.41 $\pm$ 0.20	85.72 $\pm$ 0.22	79.49 $\pm$ 0.20	73.36 $\pm$ 0.53
SCE	91.51 $\pm$ 0.24	87.65 $\pm$ 0.36	79.73 $\pm$ 0.29	61.79 $\pm$ 0.72	28.01 $\pm$ 0.92	89.54 $\pm$ 0.33	85.94 $\pm$ 0.38	80.50 $\pm$ 0.09	74.33 $\pm$ 0.56
NCE	75.48 $\pm$ 0.37	73.22 $\pm$ 0.35	69.37 $\pm$ 0.22	62.47 $\pm$ 0.85	41.20 $\pm$ 1.25	74.11 $\pm$ 0.24	72.20 $\pm$ 0.38	70.14 $\pm$ 0.27	65.33 $\pm$ 0.40
NCE+RCE	90.80 $\pm$ 0.06	88.93 $\pm$ 0.04	85.89 $\pm$ 0.31	79.89 $\pm$ 0.25	54.99 $\pm$ 2.13	90.04 $\pm$ 0.17	88.62 $\pm$ 0.29	85.07 $\pm$ 0.27	77.94 $\pm$ 0.21
NCE+AUL	91.17 $\pm$ 0.18	89.00 $\pm$ 0.58	86.05 $\pm$ 0.30	79.22 $\pm$ 0.22	56.24 $\pm$ 0.94	90.06 $\pm$ 0.16	88.19 $\pm$ 0.07	84.83 $\pm$ 0.47	77.60 $\pm$ 0.16
NCE+AGCE	91.01 $\pm$ 0.20	88.91 $\pm$ 0.38	86.16 $\pm$ 0.38	79.93 $\pm$ 0.33	43.82 $\pm$ 1.91	90.29 $\pm$ 0.05	88.49 $\pm$ 0.28	85.21 $\pm$ 0.59	78.47 $\pm$ 1.05
CE+LC	90.09 $\pm$ 0.13	83.87 $\pm$ 0.27	70.36 $\pm$ 0.23	46.53 $\pm$ 0.29	19.74 $\pm$ 1.77	87.74 $\pm$ 0.23	83.16 $\pm$ 0.33	78.48 $\pm$ 0.25	73.32 $\pm$ 0.78
ANL-CE	91.74 $\pm$ 0.18	89.68 $\pm$ 0.29	87.16 $\pm$ 0.16	81.28 $\pm$ 0.63	62.28 $\pm$ 1.10	90.66 $\pm$ 0.16	89.09 $\pm$ 0.21	85.49 $\pm$ 0.49	77.99 $\pm$ 0.40
ANL-FL	91.58 $\pm$ 0.19	89.93 $\pm$ 0.03	86.94 $\pm$ 0.03	81.10 $\pm$ 0.30	61.89 $\pm$ 2.25	<b>90.72<math>\pm</math>0.20</b>	<b>89.29<math>\pm</math>0.02</b>	85.80 $\pm$ 0.38	77.89 $\pm$ 0.28
LT-APL	-	89.42 $\pm$ 0.13	86.82 $\pm$ 0.18	80.93 $\pm$ 0.30	40.87 $\pm$ 1.57	-	89.28 $\pm$ 0.24	86.29 $\pm$ 0.36	<b>79.99<math>\pm</math>0.58</b>
<b>JAL-CE</b>	91.63 $\pm$ 0.21	<b>89.95<math>\pm</math>0.22</b>	<b>87.53<math>\pm</math>0.10</b>	<b>82.03<math>\pm</math>0.18</b>	<b>65.43<math>\pm</math>0.99</b>	90.70 $\pm$ 0.21	89.11 $\pm$ 0.38	<b>86.38<math>\pm</math>0.14</b>	<b>79.54<math>\pm</math>0.34</b>
<b>JAL-FL</b>	91.56 $\pm$ 0.25	<b>89.99<math>\pm</math>0.11</b>	<b>87.43<math>\pm</math>0.29</b>	<b>82.09<math>\pm</math>0.08</b>	<b>64.84<math>\pm</math>1.13</b>	<b>90.77<math>\pm</math>0.16</b>	<b>89.36<math>\pm</math>0.27</b>	<b>86.18<math>\pm</math>0.04</b>	79.51 $\pm$ 0.06

CIFAR-100	Clean	Symmetric				Asymmetric			
		0.2	0.4	0.6	0.8	0.1	0.2	0.3	0.4
CE	70.93 $\pm$ 0.77	56.47 $\pm$ 1.34	39.68 $\pm$ 0.77	22.64 $\pm$ 0.53	7.82 $\pm$ 0.33	64.14 $\pm$ 1.01	58.67 $\pm$ 0.45	50.44 $\pm$ 1.16	41.51 $\pm$ 0.12
FL	70.58 $\pm$ 0.34	56.32 $\pm$ 1.43	40.83 $\pm$ 0.52	22.44 $\pm$ 0.54	7.68 $\pm$ 0.37	65.00 $\pm$ 0.46	58.12 $\pm$ 0.44	51.16 $\pm$ 1.32	41.46 $\pm$ 0.38
GCE	61.73 $\pm$ 1.30	60.58 $\pm$ 2.51	57.35 $\pm$ 0.91	46.15 $\pm$ 1.10	20.33 $\pm$ 0.31	62.01 $\pm$ 1.11	59.19 $\pm$ 1.36	53.35 $\pm$ 0.65	40.92 $\pm$ 0.21
SCE	70.57 $\pm$ 0.93	55.50 $\pm$ 0.35	40.13 $\pm$ 1.48	22.23 $\pm$ 1.29	7.84 $\pm$ 0.56	64.51 $\pm$ 0.45	57.84 $\pm$ 0.57	49.66 $\pm$ 0.48	41.58 $\pm$ 0.87
NCE	29.95 $\pm$ 0.56	25.43 $\pm$ 0.91	20.26 $\pm$ 0.25	14.66 $\pm$ 1.04	8.82 $\pm$ 0.47	27.16 $\pm$ 1.01	26.67 $\pm$ 0.73	23.83 $\pm$ 0.29	20.83 $\pm$ 1.08
NCE+RCE	68.07 $\pm$ 0.70	64.57 $\pm$ 0.16	58.48 $\pm$ 0.51	46.73 $\pm$ 1.00	26.94 $\pm$ 1.29	66.74 $\pm$ 0.30	62.82 $\pm$ 0.57	55.86 $\pm$ 0.40	41.50 $\pm$ 0.39
NCE+AUL	69.95 $\pm$ 0.33	65.45 $\pm$ 0.49	56.37 $\pm$ 0.12	38.68 $\pm$ 0.75	12.95 $\pm$ 0.37	66.41 $\pm$ 0.15	57.39 $\pm$ 0.34	48.20 $\pm$ 0.19	38.41 $\pm$ 0.52
NCE+AGCE	69.05 $\pm$ 0.36	65.61 $\pm$ 0.27	59.40 $\pm$ 0.34	47.66 $\pm$ 0.49	26.14 $\pm$ 0.01	66.96 $\pm$ 0.45	64.08 $\pm$ 0.44	57.17 $\pm$ 0.33	44.62 $\pm$ 1.04
CE+LC	71.80 $\pm$ 0.34	56.26 $\pm$ 0.09	37.36 $\pm$ 0.49	17.46 $\pm$ 0.62	6.32 $\pm$ 0.16	63.51 $\pm$ 0.27	56.19 $\pm$ 0.30	48.07 $\pm$ 0.38	39.64 $\pm$ 0.14
ANL-CE	70.26 $\pm$ 0.15	66.93 $\pm$ 0.09	61.58 $\pm$ 0.33	52.09 $\pm$ 0.58	<b>28.01<math>\pm</math>1.06</b>	68.60 $\pm$ 0.41	65.96 $\pm$ 0.18	60.57 $\pm$ 0.07	45.73 $\pm$ 0.74
ANL-FL	70.11 $\pm$ 0.27	67.03 $\pm$ 0.46	61.89 $\pm$ 0.25	51.58 $\pm$ 0.33	<b>28.81<math>\pm</math>0.74</b>	68.67 $\pm$ 0.21	66.12 $\pm$ 0.39	60.03 $\pm$ 0.48	46.20 $\pm$ 0.45
LT-APL	-	63.29 $\pm$ 0.49	54.70 $\pm$ 1.73	40.52 $\pm$ 1.65	22.63 $\pm$ 0.78	-	62.59 $\pm$ 1.31	56.90 $\pm$ 1.29	44.05 $\pm$ 1.32
<b>JAL-CE</b>	70.60 $\pm$ 0.09	<b>68.25<math>\pm</math>0.39</b>	<b>64.11<math>\pm</math>0.55</b>	<b>56.73<math>\pm</math>0.65</b>	22.80 $\pm$ 2.11	<b>69.29<math>\pm</math>0.42</b>	<b>67.90<math>\pm</math>0.59</b>	<b>64.90<math>\pm</math>0.27</b>	<b>56.17<math>\pm</math>0.32</b>
<b>JAL-FL</b>	70.66 $\pm$ 0.37	<b>68.33<math>\pm</math>0.34</b>	<b>64.55<math>\pm</math>0.61</b>	<b>56.44<math>\pm</math>0.22</b>	23.11 $\pm$ 2.28	<b>69.25<math>\pm</math>0.21</b>	<b>67.63<math>\pm</math>0.50</b>	<b>65.18<math>\pm</math>0.26</b>	<b>56.26<math>\pm</math>0.05</b>

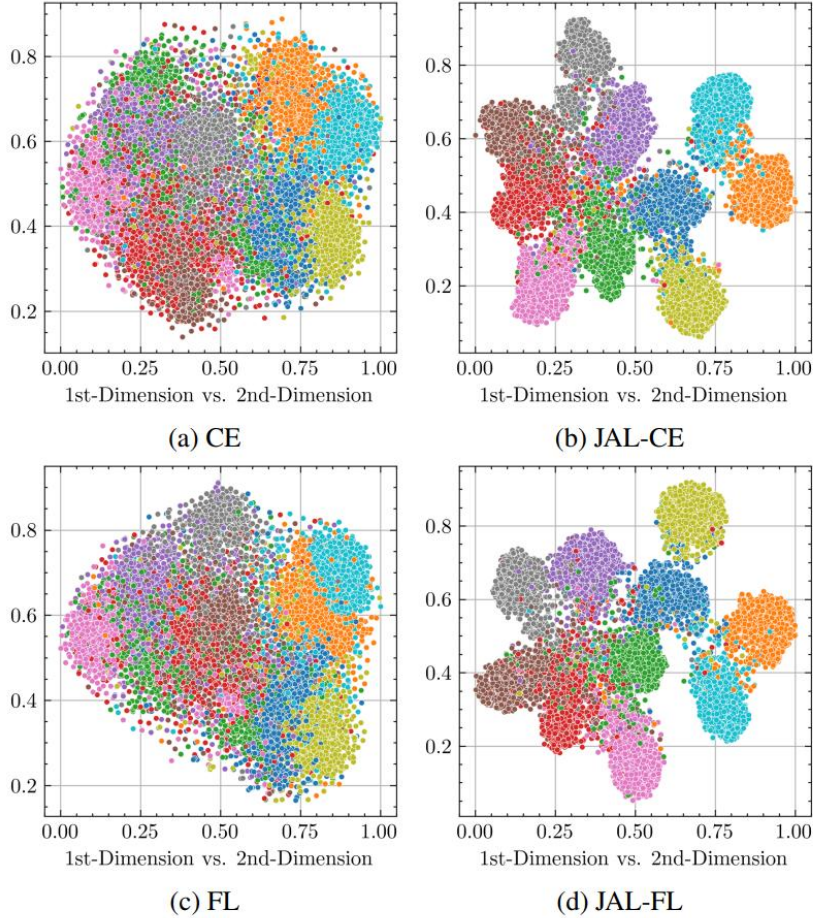


Figure 1. Visualizations of 2D t-SNE [21] embeddings of learned representations on the CIFAR-10 test set, from models trained with 0.4 symmetric noise. The representations learned by the proposed JAL method are with more separated and clearly bound margin.



# Experiments

Table 4. Last epoch test accuracies (%) of different methods on CIFAR-10 and CIFAR-100 with instance-dependent noise (IDN) ( $\eta \in [0.2, 0.4, 0.6]$ ). The results "mean $\pm$ std" are reported over 3 random trials and the top-2 best results are in **bold**.

Loss	CIFAR-10 IDN			CIFAR-100 IDN		
	0.2	0.4	0.6	0.2	0.4	0.6
CE	75.38 $\pm$ 0.19	57.63 $\pm$ 0.27	37.97 $\pm$ 0.36	57.02 $\pm$ 0.54	40.91 $\pm$ 2.05	24.49 $\pm$ 0.86
GCE	86.66 $\pm$ 0.14	79.99 $\pm$ 0.23	51.90 $\pm$ 0.13	61.43 $\pm$ 2.24	57.07 $\pm$ 1.04	42.40 $\pm$ 0.52
SCE	86.65 $\pm$ 0.27	74.54 $\pm$ 0.34	49.83 $\pm$ 0.40	56.32 $\pm$ 0.27	39.82 $\pm$ 1.43	23.19 $\pm$ 0.87
NCE+RCE	89.06 $\pm$ 0.26	85.11 $\pm$ 0.28	71.27 $\pm$ 0.66	64.33 $\pm$ 0.46	57.53 $\pm$ 0.84	40.36 $\pm$ 0.35
NCE+AGCE	88.95 $\pm$ 0.07	85.30 $\pm$ 0.23	71.49 $\pm$ 0.34	65.18 $\pm$ 0.17	57.89 $\pm$ 0.57	43.04 $\pm$ 0.29
CE+LC	82.77 $\pm$ 0.09	68.06 $\pm$ 0.22	43.60 $\pm$ 0.39	55.93 $\pm$ 0.39	37.74 $\pm$ 0.63	18.68 $\pm$ 0.50
ANL-CE	89.71 $\pm$ 0.35	85.74 $\pm$ 0.15	69.83 $\pm$ 0.38	66.89 $\pm$ 0.53	60.88 $\pm$ 0.35	48.12 $\pm$ 0.48
ANL-FL	89.68 $\pm$ 0.21	85.97 $\pm$ 0.16	70.70 $\pm$ 0.30	67.17 $\pm$ 0.11	61.07 $\pm$ 0.38	46.77 $\pm$ 0.80
<b>JAL-CE</b>	<b>90.01<math>\pm</math>0.12</b>	<b>86.46<math>\pm</math>0.15</b>	<b>75.62<math>\pm</math>0.18</b>	<b>67.51<math>\pm</math>0.29</b>	<b>63.24<math>\pm</math>0.16</b>	<b>51.69<math>\pm</math>0.68</b>
<b>JAL-FL</b>	<b>89.90<math>\pm</math>0.14</b>	<b>86.78<math>\pm</math>0.17</b>	<b>75.02<math>\pm</math>0.48</b>	<b>67.77<math>\pm</math>0.38</b>	<b>63.56<math>\pm</math>0.18</b>	<b>51.69<math>\pm</math>0.59</b>

Table 5. Last epoch test accuracies (%) of different methods on CIFAR-10N and CIFAR-100N human-annotated noise [26]. The results "mean $\pm$ std" are reported over 3 random trials and the top-2 best results are in **bold**.

Loss	CIFAR-10			CIFAR-100
	Aggregate	Random 1	Worst	Noisy
CE	85.09 $\pm$ 0.30	79.09 $\pm$ 0.28	61.43 $\pm$ 0.52	48.63 $\pm$ 0.53
GCE	87.39 $\pm$ 0.09	85.98 $\pm$ 0.42	77.77 $\pm$ 0.59	50.97 $\pm$ 0.60
SCE	88.48 $\pm$ 0.26	85.65 $\pm$ 0.30	73.65 $\pm$ 0.29	48.52 $\pm$ 0.11
NCE+RCE	89.17 $\pm$ 0.28	87.62 $\pm$ 0.34	79.74 $\pm$ 0.09	54.27 $\pm$ 0.09
NCE+AGCE	89.27 $\pm$ 0.28	87.92 $\pm$ 0.02	79.91 $\pm$ 0.37	55.96 $\pm$ 0.20
CE+LC	86.60 $\pm$ 0.40	83.51 $\pm$ 0.13	70.11 $\pm$ 0.10	47.76 $\pm$ 0.29
ANL-CE	89.66 $\pm$ 0.12	88.68 $\pm$ 0.13	80.23 $\pm$ 0.28	56.37 $\pm$ 0.42
ANL-FL	89.81 $\pm$ 0.08	88.57 $\pm$ 0.18	80.56 $\pm$ 0.23	57.09 $\pm$ 0.40
<b>JAL-CE</b>	<b>89.94<math>\pm</math>0.20</b>	<b>88.85<math>\pm</math>0.23</b>	<b>81.33<math>\pm</math>0.34</b>	<b>59.54<math>\pm</math>0.12</b>
<b>JAL-FL</b>	<b>90.06<math>\pm</math>0.22</b>	<b>88.71<math>\pm</math>0.30</b>	<b>81.25<math>\pm</math>0.10</b>	<b>59.38<math>\pm</math>0.24</b>

# Experiments

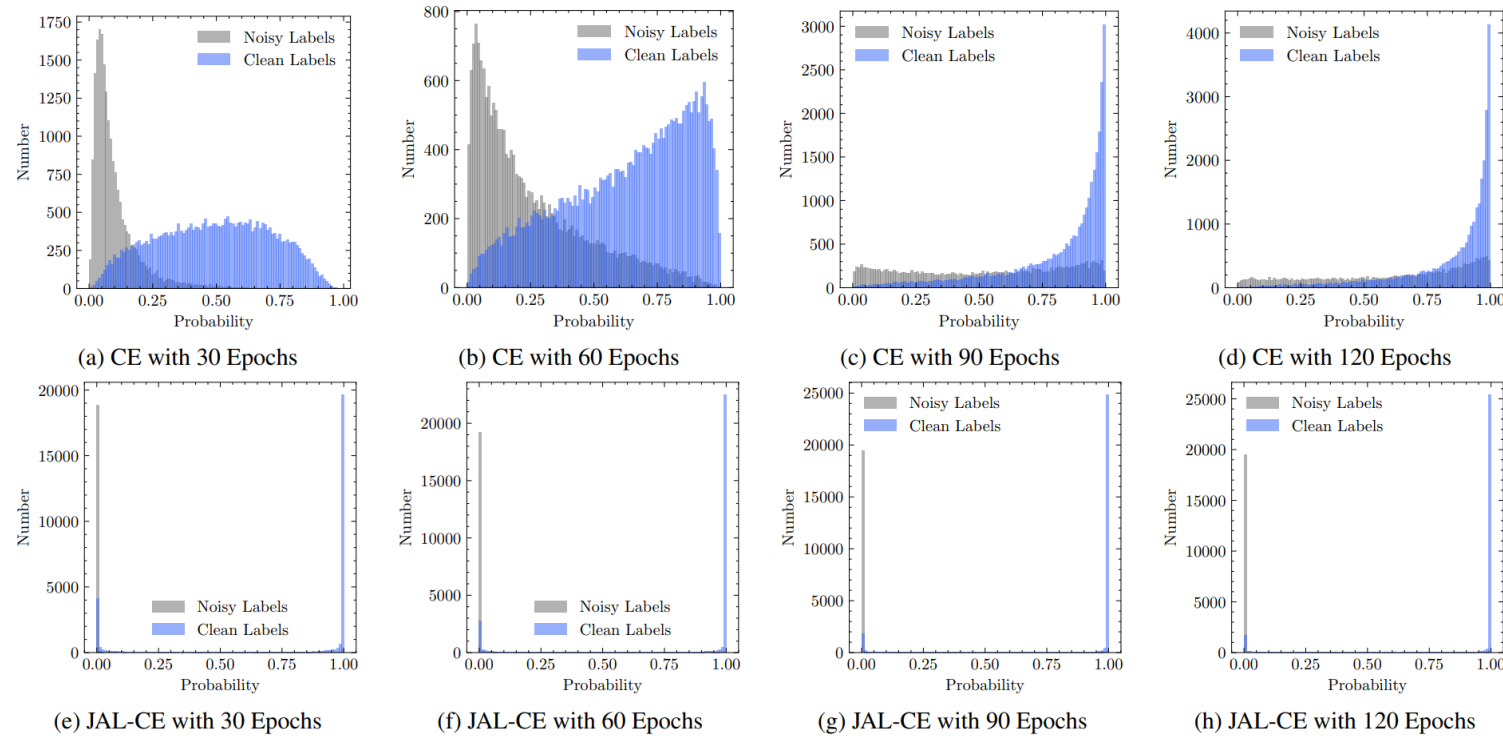


Figure 3. Histograms of the distribution of samples with different prediction probabilities in the training set for CIFAR-10 with 0.4 symmetric noise.

Table 6. Last epoch test accuracies (%) of different methods on ILSVRC12, WebVision, and Clothing1M. The top-2 best results are in **bold**.

Loss	CE	GCE	SCE	NCE+RCE	NCE+AGCE	ANL-CE	ANL-FL	JAL-CE	JAL-FL
<b>WebVision</b>	66.28	61.84	65.16	66.96	67.16	67.36	67.76	<b>69.84</b>	<b>69.20</b>
<b>ILSVRC12</b>	60.68	60.32	61.00	63.96	64.36	65.60	64.84	<b>66.64</b>	<b>66.00</b>
<b>Clothing1M</b>	67.93	68.46	67.71	69.24	67.90	69.75	69.90	<b>70.31</b>	<b>70.11</b>

# Thanks for your attention!

**Any question? Please contact us!**

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