

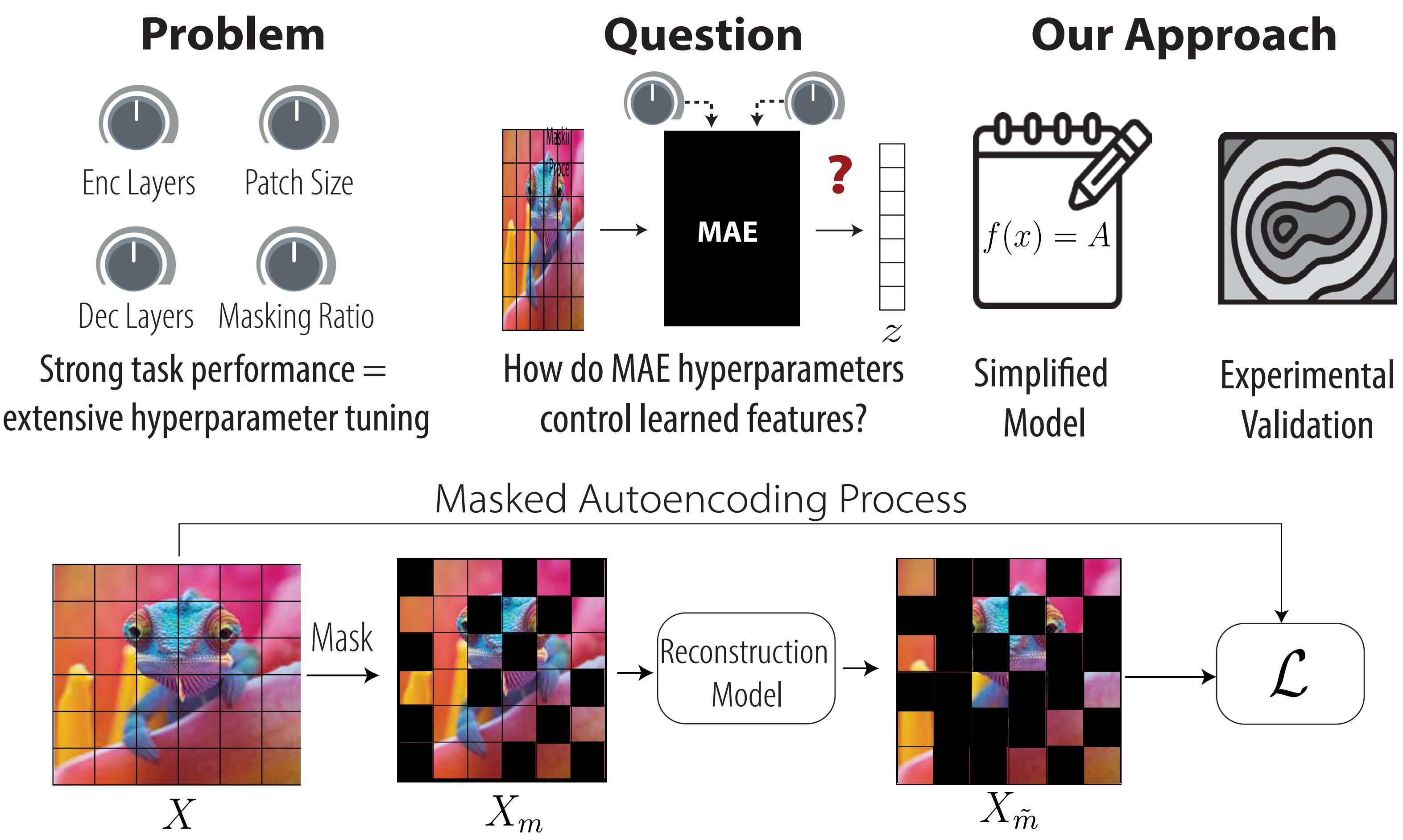
# From Linearity to Non-Linearity: How Masked Autoencoders Capture Spatial Correlations

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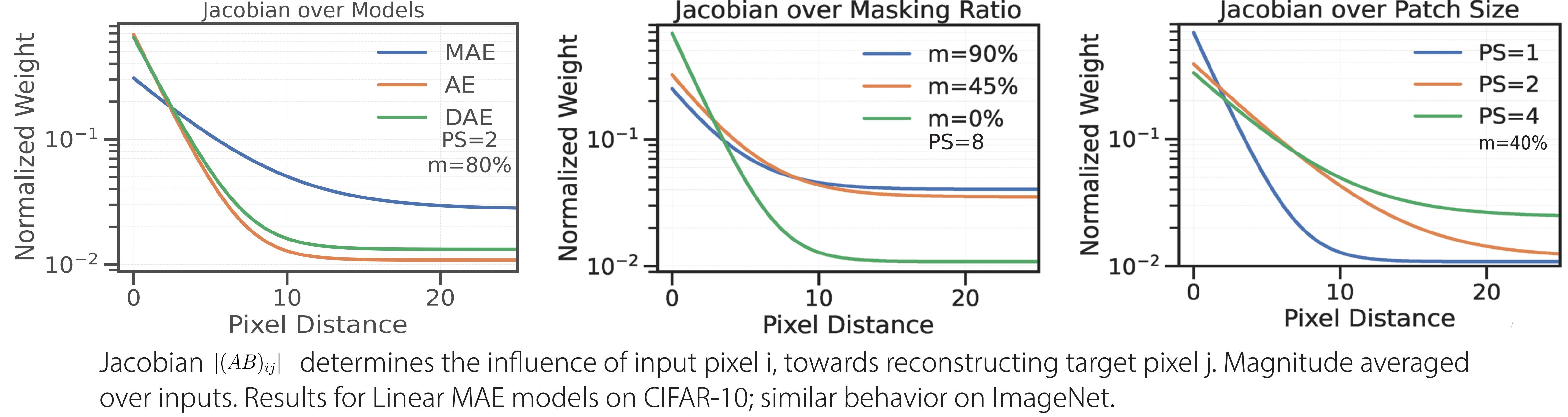
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## How should one choose MAE hyperparameters?



## How does masking shape representations in linear MAEs?

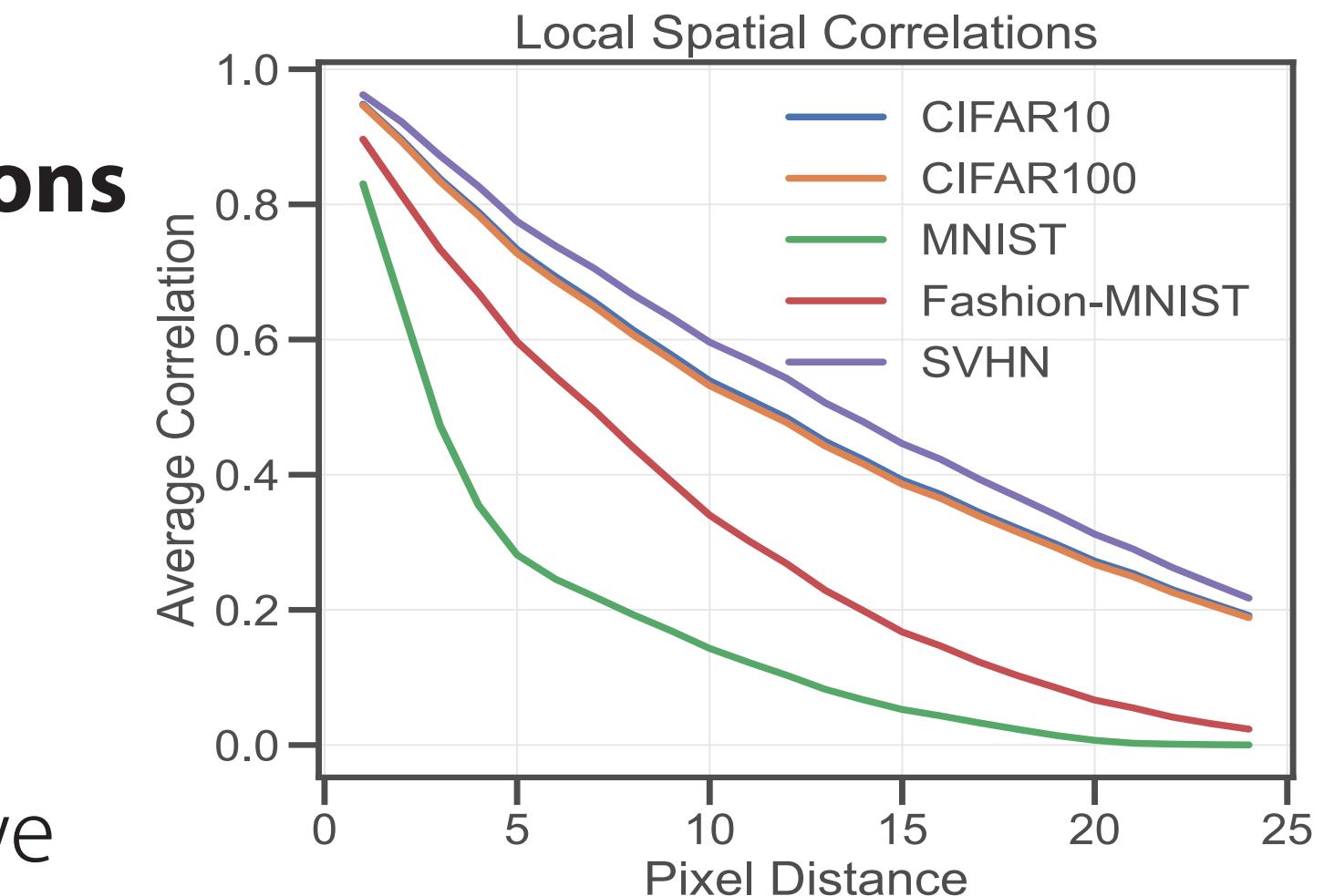


### Key Insights:

- Spatial Integration:** MAEs can integrate information from distant patches, whereas AEs and DAEs remain localized
- Patch Size Controls Spatial Extent of the Reconstruction Kernel:** Larger patches lead to broader spatial receptive fields
- Masking Ratio Controls Strength of the Regularizer:** Higher masking ratios lead to a stronger reliance on long-range spatial dependencies

## Background

- Natural images have a spatial structure: nearby pixels have **strong local correlations**



- This structure is captured in the spatial auto-correlation function:

$$R(\Delta x) = 1/N \sum_x f(x)f(x + \Delta x)$$

- By tuning patch size and masking ratio, we control the spatial correlations the model can exploit

**Takeaway: Statistical correlations in data provide regularities that MAEs can exploit to reconstruct masked regions**

## Simplified Model: Linear MAE

Data  $X \in \mathbb{R}^D$

Masking Ratio  $m$

Patch Size  $p$

$$\mathcal{L}(A, B) = \mathbb{E}_R \|X - (R \odot X)AB\|^2 \xrightarrow{\text{Expectation}} \mathcal{L}(A, B) = \underbrace{\|X - (1-m)XAB\|^2}_{\text{reconstruction}} + \underbrace{m(1-m)\|GAB\|^2}_{\text{regularizer}}$$

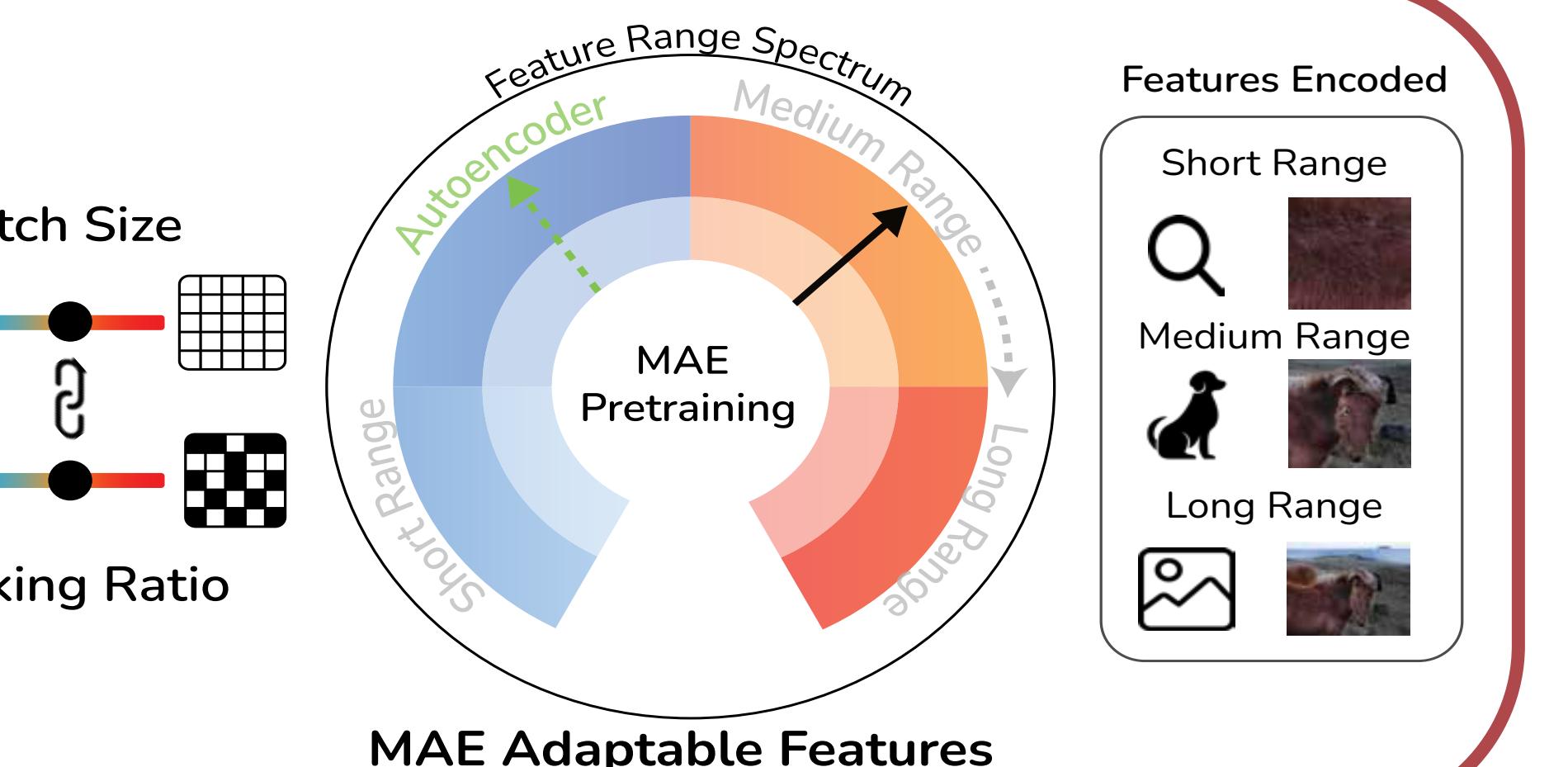
Encoder:  $A$ , Decoder:  $B$ , Mask:  $R$ , Regularizer:  $G^T G = \text{BlkDiag}_p(X^T X)$

- Marginalize linear MAE loss over masks → reconstruction + regularization (Bias of an MAE) terms → solve for closed form optimal solution

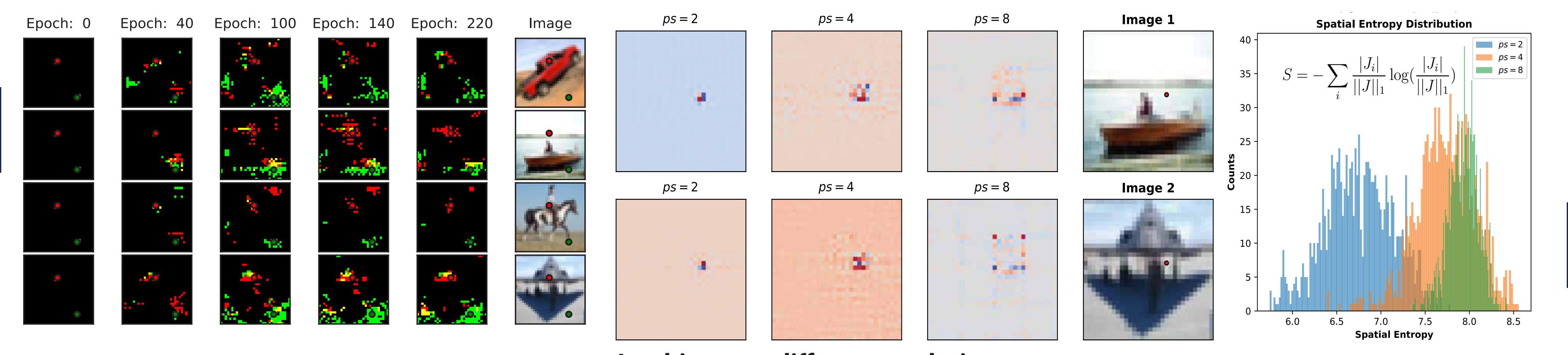
- The MAE bias makes it select features that are redundantly present across patches as opposed to an AE, which selects features that explain variance

**Takeaway: Linear MAEs acts as a data-dependent regularized autoencoder, masking ratio sets the strength, patch size controls spatial structure**

**MAEs capture spatial correlations in the data, with masking ratio and patch size controlling the spatial scale of the learned features**



## Characterizing the features of nonlinear MAEs



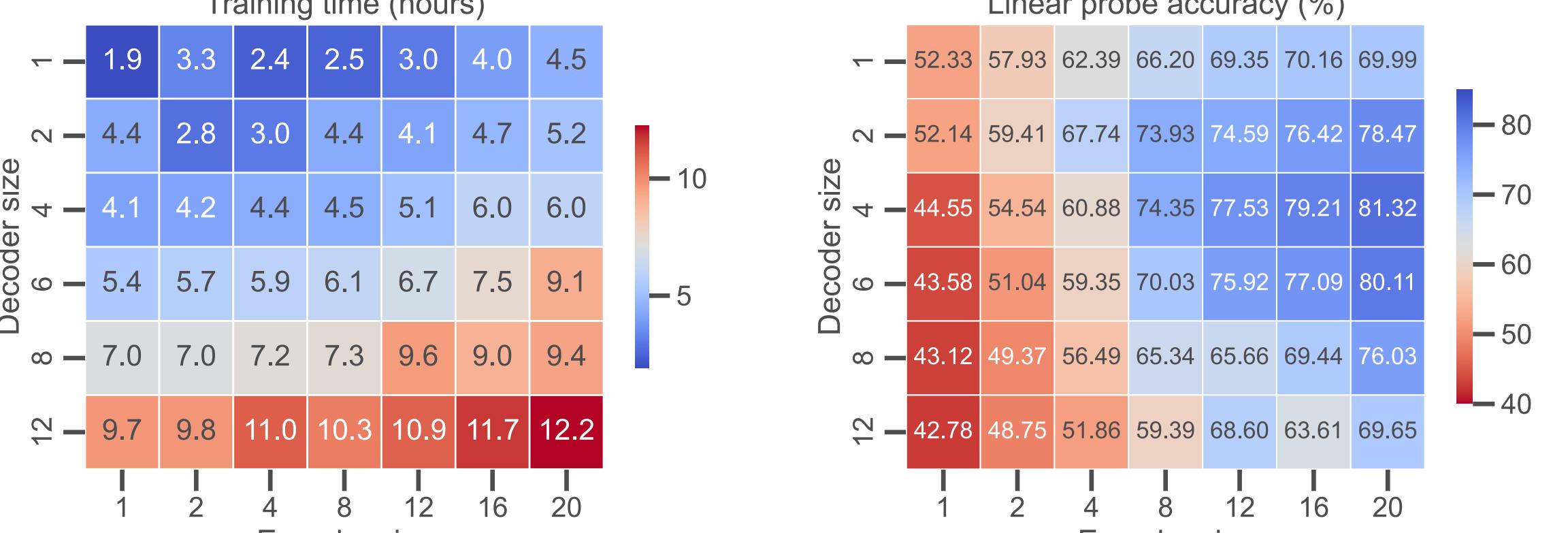
Jacobian magnitude averaged over inputs. Results shown for nonlinear models on CIFAR-10; similar behavior is observed for ImageNet

### Key Insights:

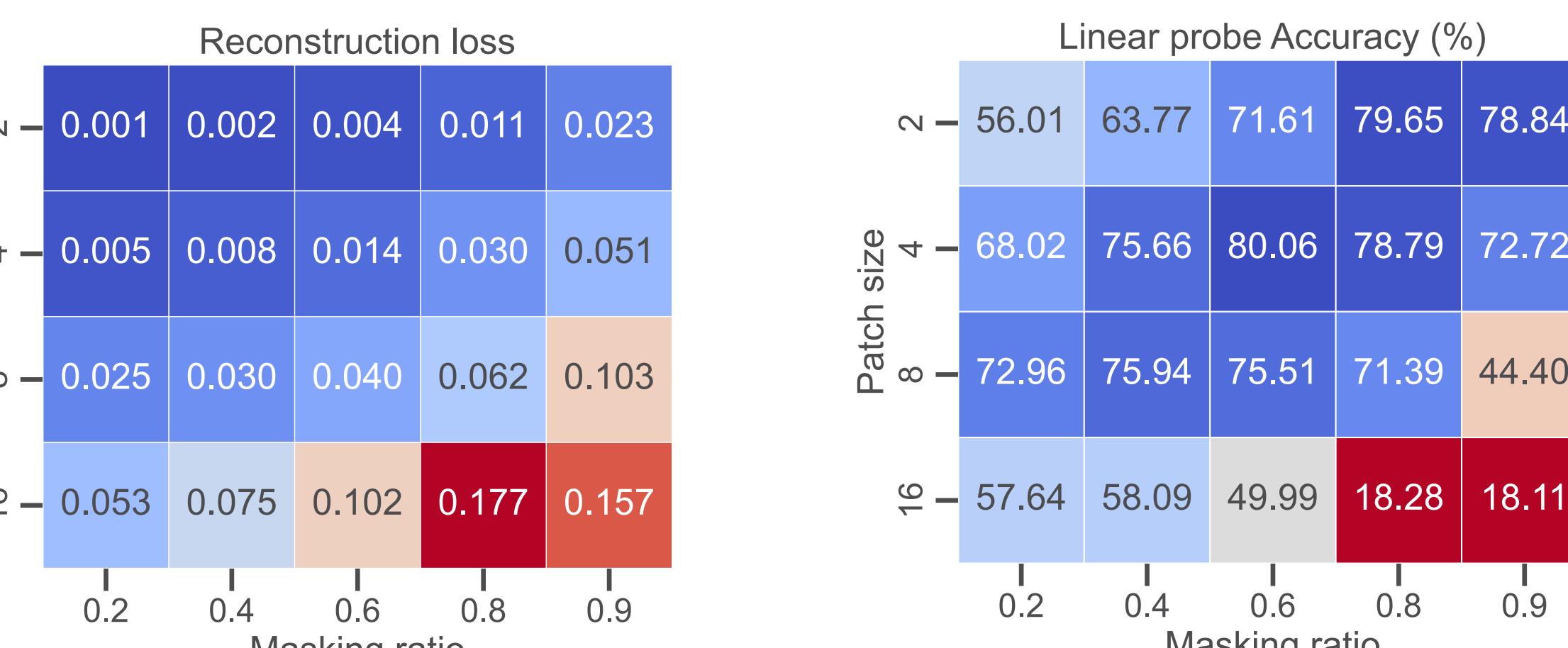
- During Training:** Jacobians evolve from highly localized kernels to become spatially diffuse
- Patch Size Controls the Spatial Extent of the Reconstruction Kernel:** Larger patch sizes yield reconstruction kernels with higher spatial entropy, shifting from local to global information aggregation
- MAEs provide a potential mechanism for ViTs to learn local receptive fields

## How to train your MAE

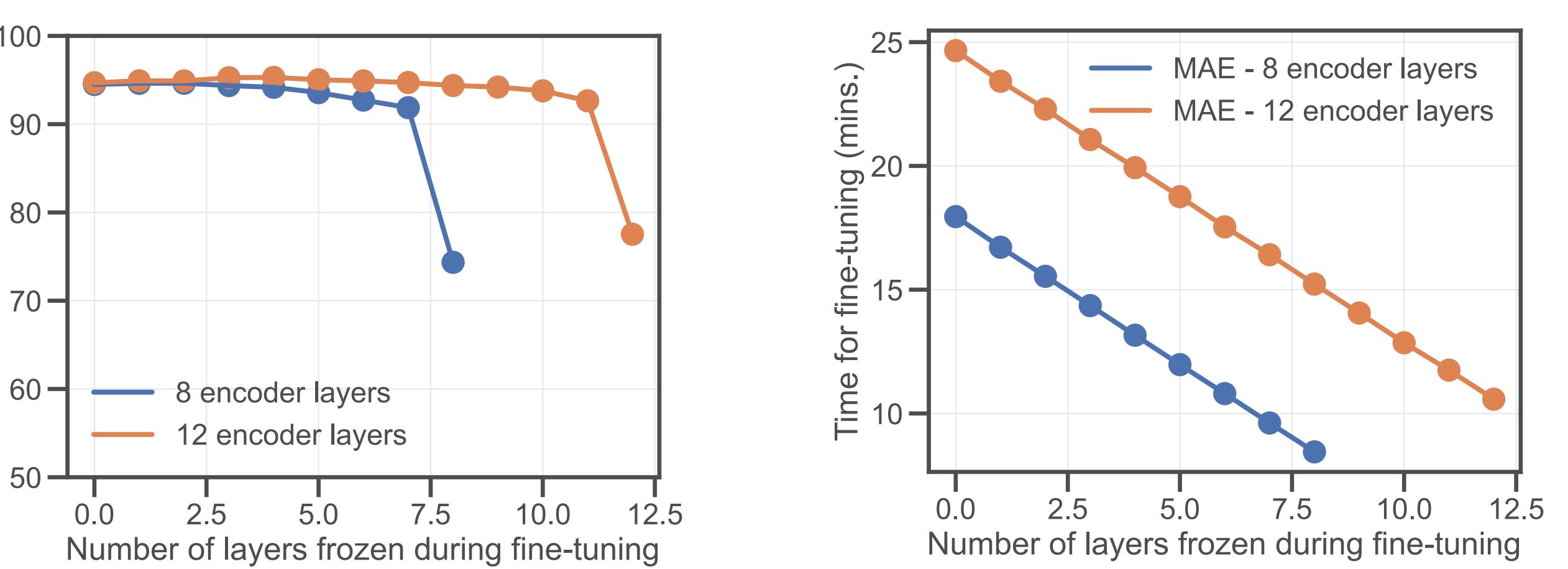
**MAEs Benefit from Deeper Encoders and Minimal Decoders, Achieving Near Fine-Tuning Accuracy at 4x Faster Training Speed**



**Bigger Patches, Less Masking: Optimal MAE Performance Shifts Toward Lower Masking Ratios with Increasing Patch Size**



**Fine-Tuning Only a Few MAE Layers Achieves Near-Full Accuracy with Half the Training Cost**



CIFAR-10 with 192 embedding dimensions pretrained for 2000 epochs with AdamW, and fine-tuned for 100 epochs

## Conclusion

**Hyperparameters determine the scale of the learned features:**  
 Masking ratio and patch size set how broadly MAEs integrate spatial structure

**Key Question:** How do spatial correlation scales relate to useful features for perception tasks?

- For example, tasks such as optical flow require large spatial scales to overcome the aperture problem